

# Calibration of Model Uncertainty for Ensemble Forecast of Ionosphere Conditions

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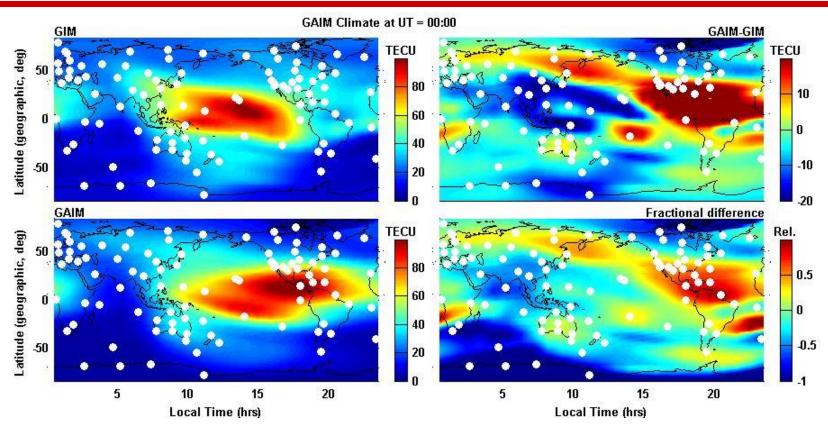
### **Ensemble Forecast Must Realistically Represent Model Uncertainties**

- Ensemble technique allows propagation of uncertainty from suspected sources to model states
- Random or strategic sampling are based on underlying uncertainty models
- Ensemble forecast or data analysis must correctly represents statistical characteristics of the model state such as means and covariance
- Improvement of forecast reduces uncertainty

Calibrated Uncertainty Ensures Realism of Ensemble Forecast



### **Comparison with Data Driven Models Shows Larger Diversity in Data**



Model must be able to produce observed variability



#### First Principle Numerical Model is the Primary Tool for Forecast

- GAIM climate model is a first principle, multiple ion model for mid and low latitude region of ionosphere
- Model was developed with data assimilation as part of its design
- Parameterization of driver perturbation and solution of the adjoint equation allows implementation of 4DVAR for driver estimation
- Both Kalman and 4DVAR versions of the JPL/USC GAIM are based on the same first principle model



#### Model Uncertainty Inherently Corresponds to Unmodeled Physics

- Approximation of physical laws
  - Simplification of physical laws
  - Spatial and temporal discretization
  - Relatively easy to quantify
- Unknown model parameters
  - Ionosphere drivers such as solar irradiance, neutral density, temperature and velocity
  - Initial conditions of the system
- Unknown mechanism influencing the dynamics

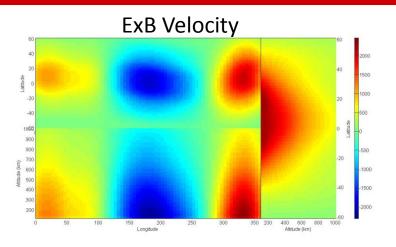


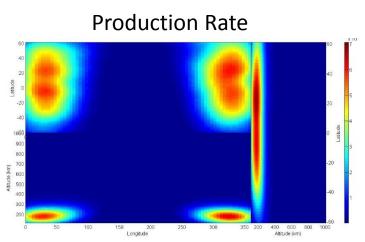
#### Primary Sources of Uncertainty Come from Unknown Parameters

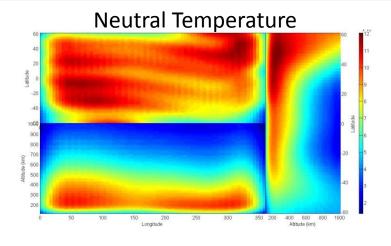
- Model of the ionosphere strongly dependent on external driving forces that are poorly known
- Statistical values of these parameters are often used in forecast model
- Effect of randomness of driver parameters on the model states are mostly nonlinear and globally correlated
- Understanding of the uncertainty can lead to improvement of forecast and data assimilation

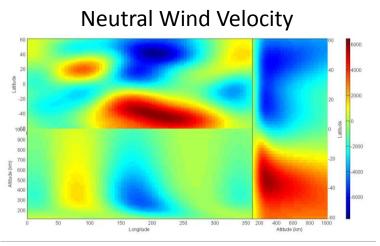


#### Number of Parameters Provides Sufficient Degree of Freedom



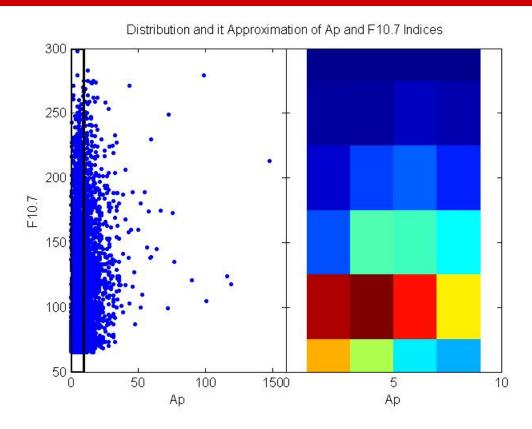








#### **Ensemble Based on Solar Indices Serves** as Baseline for Forecast Performance

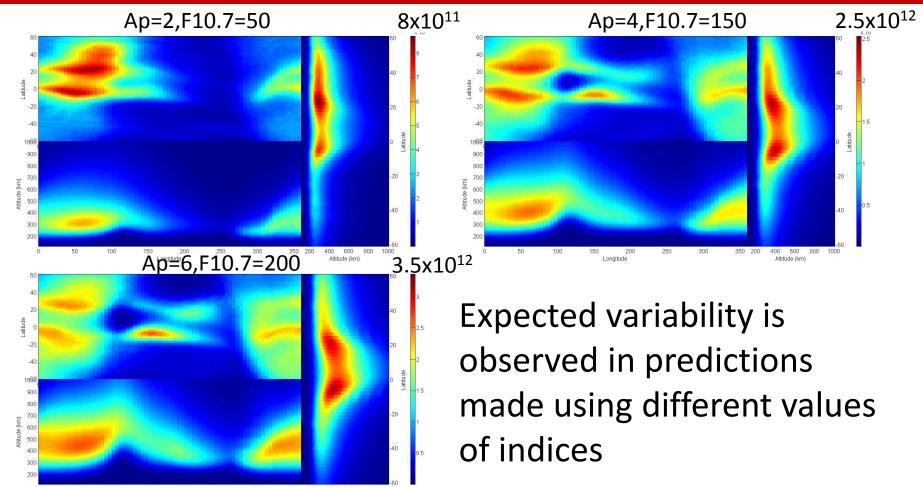


Sampled area represents over 60% of quite conditions. Index data from 1997-2012

- "Prediction" is for April 25, 2011
- Ensemble of index values covers large number of historic cases
- Limit data to solar minimum conditions or data from a specific season reduces diversity



## Large Scale Changes Are Reproduced by the Ensemble Forecast





#### First Principle Analysis Identifies Key Components of Deviation from Mean

- Small ensemble size does not allow accurate characterization of covariance of model prediction
- Principle Component Analysis computes singular vectors of the empirical covariance matrix
- The leading Principle Components may still be representative of the main characteristics of the deviations from the ensemble mean
- Principle Components form an orthonormal basis that captures all deviations from mean



### Principle Component Analysis Helps Quantifying the Degree of Variability

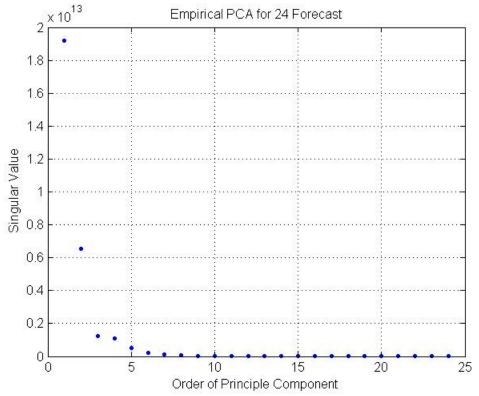
PCA can be relatively easy to perform when the ensemble size is small

$$D = [f_1, \dots, f_n], T = D^T D, T v_k = s_k^2 v_k$$
$$PC_k = D v_k$$

- Singular values  $s_k$  represents the degree of variation of the projection onto the associated PC
- When the values of  $s_k$  drop off rapidly, the data has low overall variability



#### Only a Very Small Number of Principle Values are Over 1%

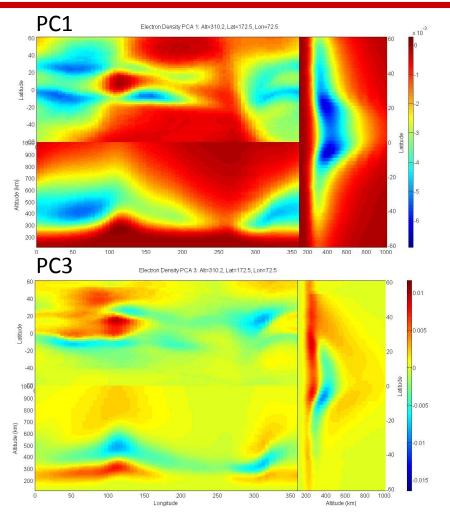


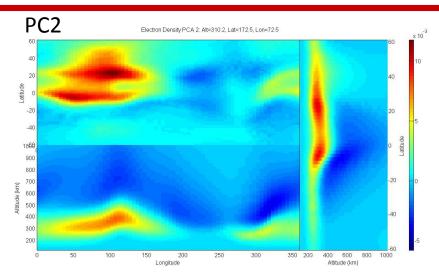
Principle Components of deviation from ensemble mean is also affected by the selection of the ensemble

- Singular values of relative to the leading SV provides significance of the PC
- Principle components may be linked to specific weather effect
  - The most interesting weather event may by linked to secondary PCs



### Principle Components Show Interesting Features

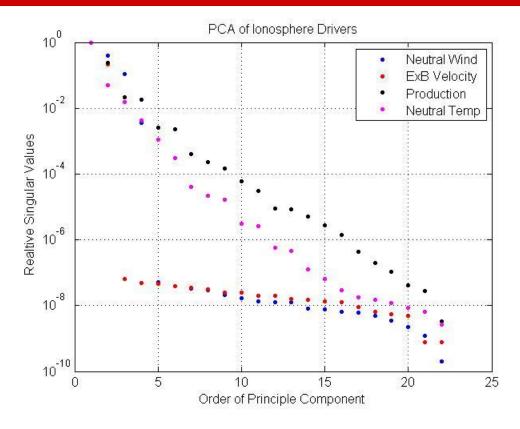




 The leading components shows nonlinear effects of random drivers: mean field is larger than most data at noon local time



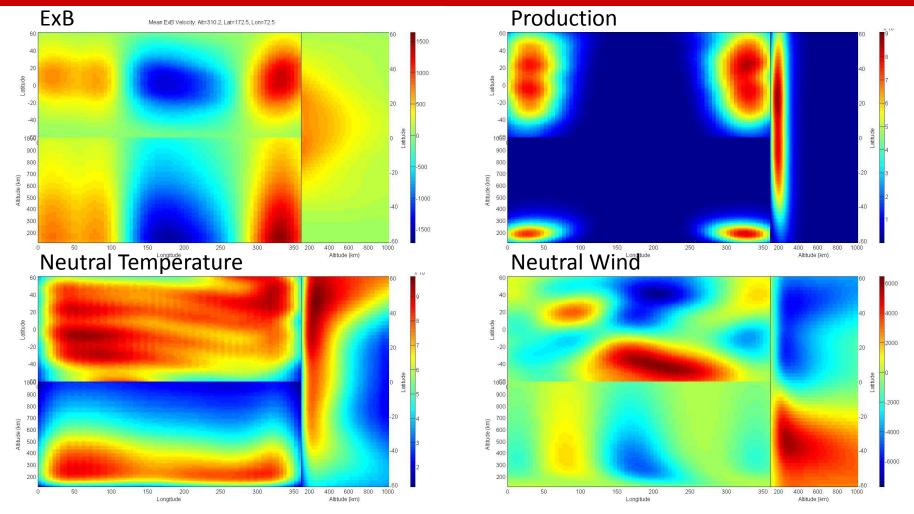
#### Small Number of Significant PCs May be Due to Small Driver Variability



- Sample of 4 key drivers shows less than 5 PC with larger than 1% of relative singular values
- Alternative driver models may lead to additional variability

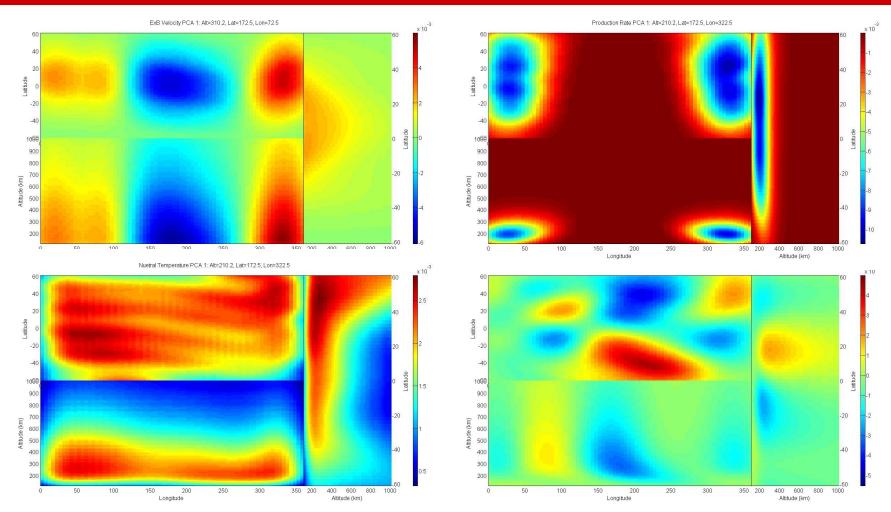


#### Mean Driver Fields Represent the Overall Characteristics





#### Leading Principle Components of Driver Fields Are Dominant





### Small Variability in Model Output Limits Ability to Forecast

- Is small variability inherent in any model that relies on a small number of observations of space environment?
- Can ensemble of models for the drivers help address the problem of small variability?
- How can we calibrate variability due to unmodeled physics in ionosphere and its drivers?
- Does data assimilation offer hope for increasing variability in driver and model output?



#### **Conclusion**

- Simple ensemble forecast experiment reveals low model variability of climatological models for drivers and ionosphere electron density
- Characterization of the principle components based on ensemble simulation shows interesting features
- Identifying the principle components of the drivers can significantly improve efficiency and accuracy of ensemble forecast
- Current analysis can be applied to other models